#### Abstract

This paper applies the MPI-OpenMP-based two-dimensional Hopmoc method using the explicit work-sharing technique with a recently proposed mechanism to reduce implicit barriers in OpenMP. Specifically, this paper applies the numerical algorithm to provide approximate solutions to the advection-diffusion equation. Additionally, this article splits the mesh used by the numerical method and distributes them to over-allocated threads. The mesh partitions became so small that the approach reduced the cache miss rate. Consequently, the strategy accelerated the numerical method in multicore systems. This paper then evaluates the results of implementing the strategy under different metrics. As a result, the use of the set of techniques improved the performance of the parallel numerical method.

### HOPMOC versions



(a) Pseudocode excerpt of parallel Hopmoc method using naive MPI-OMP

Figure 1: Two distinct implementations of th Hopmoc method

## Experiment performed on a Intel<sup>®</sup> Xeon<sup>®</sup> processor E5-2698 machine (32 physical cores)



(a) Speedups from executions of naive and MPI-OMP-EWS implementations of the two-dimensional Hopmoc method varying the number of threads from 1 to 1,100 threads.

Figure 2: Speedup and LLC miss count

Reducing cache miss rate using thread overallocation to accelerate the MPI-OpenMP-based 2-D Hopmoc method 1 - National Laboratory of Scientific Computing (LNCC), 2 - Federal University of Lavras (UFLA)

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2	Each MPI process computes its partition mesh
3	Each OMP thread computes its local
4	mesh inside the partition mesh allocated to a process
5	while $time < FinalTime$ do
6	
7	lock
8	for columns in the thread local mesh do
9	<b>for</b> all lines in the input mesh <b>do</b>
10	MMOC or an explicit or implicit time semi-step
11	end
12	end
13	unlock
14	Each OMP thread waits for its neighbours
15	
16	end
17 e	end

(b) Pseudocode excerpt of parallel Hopmoc method using MPI-OMP-EWS

(b) LLC miss count from executions of naive and MPI-OMP-EWS implementations of the two-dimensional Hopmoc method varying the number of threads from 1 to 1,200 threads

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(a) L1 cache miss count from executions of naive and MPI-OMP-EWS implementations of the two-dimensional Hopmoc method varying the number of threads from 1 to 3,200 threads

(b) L2 cache miss count from executions of naive and MPI-OMP-EWS implementations of the two-dimensional Hopmoc method varying the number of threads from 1 to 3,200 threads

Figure 3: L1 and L2 cache miss counts



Figure 4: Speedups from executions of naive and MPI-OMP-EWS-based implementations of the two-dimensional Hopmoc method varying the number of threads from 1 to 3,744 threads.

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